

## ERRATA IN AND COMMENTS ON MILNE'S NOTES ON ABELIAN VARIETIES

- p.10,  $A(\mathbb{C})$
- p.11,  $Z$  instead of  $\mathbb{Z}$
- p.13, It might be helpful to mention the identity  $\bigwedge^r(V \oplus W) = \bigoplus_{i+j=r} \bigwedge^i(V) \otimes \bigwedge^j(W)$  either in the proof of Theorem 2.3, where it is used implicitly, or before when you introduce the exterior product
- p.14, *but it is says*
- p.15, *on E* on  $X$
- p.15, polarizable *tori is*
- p.15, for a simply polarizable torus  $X$
- p.18,  $Im(\phi^*)$ , the wrong phi
- p.18, the intersection in the proof of Lemma 3.5 should have a  $U$  instead of  $C$
- p.18, passing *through P*
- p.19, *From the (3.5)*
- p.20, the proof of 3.9 doesn't contain the case of  $\mathbb{P}^1$
- p.22,  $m, m, q, \dots, q, 0$  should have a  $p$  in it, too, for clarity
- p.23, proof of 5.4: the use of  $n$  is slightly confusing, because you use it both as the induction variable, and in (2), so when you say *Take  $n = 1$* , you're proving the statement for  $n = 2$
- p.26, in the proof of 5.16: *see (5.10)*
- p.26, later the reference should probably be *After (5.13)*, and later 5.19 instead of 5.18
- p.29, I personally found the proof of 6.1 confusing on a first read, in particular, the existence of  $D_i$
- p.33, proof of 7.2:  $\mathcal{L} \otimes (-1)_A^* \mathcal{L}$  is also *very* ample
- p.33, *it is once remove*
- p.35, *Because,*
- p.35, *that that*
- p.35,  $\lambda_D = (\deg D)^2 \lambda_D$
- p.35,  $\lambda_{\mathcal{L}} = 0$ . (the dot is missing)
- p.36, in 8.6.,  $C = A$
- p.36, *Picard, variety*
- p.37, in line 3, it would be good to add that  $\mathcal{L}$  is defined on  $A \times T$
- p.37, there is a regular map  $\alpha : T \rightarrow A^\vee$ , not  $A$
- p.37, (5.37)
- p.39, first line,  $U$  should be the complement of  $V \cap H$
- p.39, *nor the 2 by a 1* is slightly misleading, should be *nor by 1*
- p.40,  $\phi$  should be replaced by  $\lambda$
- p.40, in the last line of the first paragraph, should read  $(\mathcal{L}^*)_a \approx (\mathcal{L}^*)_b$
- p.40, *it is now subgroup*
- p.40, *proved very general theorem*
- p.43,  $\Phi$  instead of  $\psi$  at the end of 10.2
- p.44, at the end of the proof of 10.3, the basis should be indexed by  $(1, \dots, d)$ , not  $e_1, \dots, e_n$ , similarly for the  $e'_i$
- p.44,  $A(k^{\text{sep}})(l)$  has not been defined
- p.46, *a field an arbitrary field..*
- p.46, *so it natural*
- p.46, in the second half of the page, the standing hypothesis is that  $A$  is defined over  $\mathbb{C}$ , which should be replaced by  $k$
- p.47, in 10.13, *function of degree 2g in*, should be *on*.
- p.48, in the proof of 10.13, need also to show that the polynomial is non-trivial
- p.48, in the proof of 10.9, I'm not sure how you obtained the summand  $(\alpha + n_A)^* D$  in your formula for  $D_n$ , and the notation is a bit confusing, because it seems you take  $\alpha = 1$  and  $\beta = \alpha$  in the formula derived in the proof of 10.13
- p.49, *The contradicts*

- p.50, *Faltings proved in*, an *it* is missing
- p.50, a space between *group* and  $\text{NS}(V)$
- p.52, proof of 10.20:  $k = k^{\text{sep}}$ , not  $k_s$
- p.52,  $\text{Trd}$ , not  $\text{Trd}$
- p.52, in 10.23, what's  $\alpha$ ?
- p.53, *We shall that*
- p.53, the characteristic polynomial of  $\alpha$ , not  $V_l(\alpha)$
- p.53, in *Notes*, there shouldn't be an  $n$  in  $A(l^n)$  (4 times), and it should be isomorphic to  $(\mathbb{Q}_l/\mathbb{Z}_l)^{2 \dim A}$  not  $(\mathbb{Q}_l/\mathbb{Z}_l)^{\dim A}$
- p.54, the reference should be Theorem 11.1, not 10.1
- p.54, *Lefschetz traces formula*
- p.54, *then  $\text{End}^0(A)$  a division*
- p.54, later need to tensor  $\text{End}^0(A)$  with  $\mathbb{Q}_l$  to compare to  $M_2(\mathbb{Q}_l)$
- p.55, in 12.1(b):  $\mathbb{Z}_l$  not  $Z_l$
- p.56, *dimension if*
- p.56, the map  $\bigwedge^r H^1(A, \mathbb{Z}_l) \rightarrow H^r(A, \mathbb{Z}_l)$  is injective, not to  $H^1$
- p.56,  $n > 0$  *prime to  $n$*
- p.56, in 12.5.,  $k$  separably closed was precisely the assumption of 12.1
- p.58, in 13.2(c), it should be  $\alpha^* \mathcal{L}$ , not  $\alpha * \mathcal{L}$
- p.58, in the exact sequence, the second to last 1 should be a 2
- p.59, in the first line, should use homology, not cohomology
- p.59, in the proof of 13.5, apply the *theorem*
- p.59, it should be  $e_{mn}(a, \lambda b') = e_{mn}(c, \lambda b')^n$ , not  $e_{mn}(c, \lambda b)^n$
- p.61, in the proof of 13.13, the quoted theorem should be (15.3), not (15.1)
- p.63, in 14.6(b): can you elaborate on how  $K$  is used?
- p.63, second to last line:  $\lambda \mapsto u^\vee \circ \lambda \circ u$
- p.64, second line: *the  $u^* \mathcal{L}$  should be then*
- p.66, *we are given mapping*
- p.66, *interpret*
- p.67, in 16.1,  $\alpha = f$
- p.68, in the proof of 16.4(a),  $B$  is undefined
- p.68, *the images the*
- p.68,  $\alpha_2(B_2)$ , not  $\alpha_2(B)$
- p.71, *integral of the form,*
- p.71, *a elliptic*
- p.72,  $\int_\gamma \omega = a \int_\gamma \omega$  should be a sum over  $i$
- p.73,  $\mathbb{Z}$  instead of  $Z$ .